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**Course: Econometrics 512**

**Problem Set 4**

**Problem 1:** Verify the measurement error result.

 (1)

Where

 (2)

Where

 (3)

Where

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| **Table 1: Measurement Error Regression Estimation** | | | | | | |
| ()=-0.03064272 | |  |  | ()=0.011488510 | |  |
|  |  | |  | |  | |
| Dependent: Y | Coefficient | P>|t| | Coefficient | P>|t| | Coefficient | P>|t| |
|  | -0.061285 | 0.566000 | 0.011489 | 0.706000 | 0.0346435 | 0.246000 |
| Constant | 9.998374 | 0.000000 | 9.962787 | 0.000000 | 9.9496940 | 0.000000 |
|  | N=1000 | | N=1000 | | N=1000 | |
|  | R-squared =0.0003 | | R-squared=0.0001 | | R-squared=0.0014 | |
|  | F-Stat=0.33(0.5660) | | F-Stat=0.14(0.7063) | | F-Stat=1.35(0.2455) | |



**Question (a):** If you run a regression of on you get something close to

**Interpretation:**

The regression analysis shows that when  is regressed on , the treatment has an insignificant negative impact on . The implication of this result is that when the unobserved  is assumed to follow a uniform distribution, it is insignificant to the model as shown in Table 1. **Appendix 1** contains the **STATA output** for this question and also the **STATA codes** are shown in **Appendix 8**.

**Question (b):** If you run a regression of and  you get something close to 

**Interpretation:**

The regression analysis showed that when  is regressed on  , has an insignificant positive effect on . Also, the value of the estimated parameter (0.011489) of this model is equal to = 0.01148851. The implication is that when the noisy version of is observed the estimated parameters are equal, indicating the impact of i.i.d measurement error with variance on the model. **Appendix 2** contains the **STATA output** for this question and also the **STATA codes** are shown in **Appendix 8**.

**Question (c):** Doing IV using  as an instrument for gives an estimate close to 

**Interpretation:**

Table 1 also shows the result, which answer this question. The result shows that when is used an instrument in this model, it has an insignificant positive impact on . The estimated value here (i.e.0.0346435) is close to ()=-0.03064272 in the absolute term. The implication is that when is correlated with but uncorrelated with error term the esitimated parameter is closed to . **Appendix 3** contains the **STATA output** for this question and also the **STATA codes** are shown in **Appendix 8**.

**Problem 2:** How bootstrapping affect standard error estimation in an IV setting.

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| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| **Table 2: Linear Regression and IV Regression Estimations with and without Bootstrapping** | | | | | | | | | | |
|  | OLS(N=711) | | OLS-Bootstrap (Replications=1000) | |  | IVR(N=2588) | | IVR-Bootstrap (Replication=1000) | |
|  | R-squared=0.0465 | | R-squared=0.0465 | |  | R-squared=0.0174 | | R-squared=0.0174 | |
|  | F-Stat=4.06(0.0002) | | Waldchi2=20.21(0.0051) | |  | Waldchi2=49.49(0.000) | | Waldchi2=9.50(0.2187) | |
| Variables | Coefficients | Robust Std. Err. | Coefficients | Bootstrap Std.Err. | Variables | Coefficients | Robust Std. Err. | Coefficients | Bootstrap Std.Err. |
| Pct\_insclnxtyr | -0.051748  (0.001) | 0.015011 | -0.051748  (0.004) | 0.017789 | ctuition17 | 0.825821  (0.000) | 0.220123 | 0.825821  (0.099) | 0.500323 |
| Mhighgrad | 1.705758  (0.135) | 1.138679 | 1.705758  (0.207) | 1.350351 | mhighgrad | 1.714111  (0.006) | 0.620411 | 1.714111  (0.227) | 1.418963 |
| msomcol | 1.654315  (0.185) | 1.249697 | 1.654315  (0.257) | 1.460228 | msomcol | 1.641105  (0.011) | 0.647933 | 1.641105  (0.254) | 1.439741 |
| fhighgrad | 2.047867  (0.082) | 1.175058 | 2.047867  (0.135) | 1.371592 | fhighgrad | 0.346595  (0.580) | 0.626745 | 0.346595  (0.808) | 1.429186 |
| fsomcol | -0.694729  (0.586) | 1.274121 | -0.694729  (0.657) | 1.565226 | fsomcol | -1.267924  (0.064) | 0.685348 | -1.267924  (0.418) | 1.564162 |
| parincome | 0.015601  (0.074) | 0.008707 | 0.015601  (0.145) | 0.010704 | parincome | 0.008082  (0.015) | 0.003311 | 0.008082  (0.294) | 0.007051 |
| afqt | 0.025462  (0.115) | 0.016147 | 0.025462  (0.163) | 0.018246 | afqt | -0.02129  (0.0104) | 0.008217 | -0.021294  (0.246) | 0.018361 |
| Constant | 4.478025  (0.001) | 1.398370 | 4.478025  (0.007) | 1.661462 | constant | 2.573612  (0.000) | 0.602760 | 2.573612  (0.054) | 1.333937 |

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| **Table3: Mean Estimation** | | | | |
| N=1000 | | | | |
| Variables | Mean | Std.Err. | (95% Conf. Interval) | |
| Pct\_insclnxtyr | -0.0524788 | 0.0005625 | -0.0535827 | -0.0513749 |
| ctuition17 | 0.8145842 | 0.0158216 | 0.7835368 | 0.8456315 |

**Question(a):** Estimate the regression via OLS with robust standard errors (based on the usual asymptotic approximation accounting for generic heteroskedasticity). Report the 95% confidence interval for the variable “pctinsclnxtyr”.

**Interpretation:**

Table 2 presents the result to this section. In assessing the relationship between the exogeneous variables in this model and the dependent variable, the result shows that Pct\_insclnxtyr, fhighgrad, and parincome have different significant impact on dayssmklm17. In addition, the robust standard error result as shown in table also support our findings. However, other variables in this model are insignificant to impact dayssmklm17. Furthermore, as shown in Appendix, we are 95% confident that the estimated value of Pct\_insclnxtyr fall between -0.0812201 and -0.022751. **Appendix 4** contains the **STATA output** for this question and also the **STATA codes** are shown in **Appendix 9**.

**Question(b):** Now estimate the standard errors by using the non-parametric bootstrap. This involves re-sampling observations with replacement (until you have N observations, where N is the numb er of observations in the regression), estimating the model, saving the coefficient, and then doing this many times over (you should use 1,000 replications in each of these exercises). You can then compute standard errors or do hypothesis testing based on the distribution of the coefficients. This is sometimes called the “bootstrap-c”, where “c” stands for coefficient. If you use Stata, look at the “bootstrap” command. Remember to set a seed for replication purposes (since bootstrapping is based on a random process, you won't get the same answer every time unless you set the seed). Report the 95% confidence interval for the variable “pctinsclnxtyr”.

**Interpretation:**

Table 2 also presents the result of the bootstrapping OLS. In assessing the relationship between the exogeneous variables in this model and the dependent variable, the result shows that while others variables are insignificant to the model, Pct\_insclnxtyr, significantly impact on dayssmklm17. In addition, the robust standard error result as shown in table also support our findings that Pct\_insclnxtyr is very important to the model. Furthermore, as shown in Appendix, we are 95% confident that the estimated value of Pct\_insclnxtyr fall between -0.0866 and -0.01688. **Appendix 5** contains the **STATA output** for this question and also the **STATA codes** are shown in **Appendix 9**.

**Question (c)**

Now repeat parts (a) and (b) but with IV estimation, using “ctuition17” as an instrument for “pctinsclnxtyr”.

**Interpretation:**

For the IV estimation with bootstrapping, Table 2 also presents the result. The result shows that ctuition17, mhighgrad, msomcol, fsomcol, parincome, and afqt significantly have impact on dayssmklm17. The implication of this result is that IV estimation is very robust for these data. Furthermore, as shown in Appendix, we are 95% confident that the estimated value of ctuition17, fall between -0.3944 and 1.2573. Similarly, Table 2 also presents the result of the bootstrapping IV estimation, the result shows that while other variables are insignificant to the model, ctuition17, significantly impact on dayssmklm17. In addition, the robust standard error result as shown in table also support our findings that ctuition17 is very important to the model. Furthermore, as shown in Appendix, we are 95% confident that the estimated value of ctuition17 fall between -0.1548 and 1.8064. **Appendix 6 and 7** contains the **STATA output** for this question and also the **STATA codes** are shown in **Appendix 9**.

**Question (d)**

A new and important paper by Alwyn Young (presented in class) suggests that bootstrapping may provide more accurate inference in IV settings than traditional asymptotic inference (even when adjusting for heteroskedasticity or correlated errors). Why is IV especially susceptible to these problems in finite samples (relative to OLS)?

**Interpretations**

The following explain the reasons

1. Non-iid error processes adversely affect the size and power of IV estimates, increasing the bias of IV relative to OLS.
2. 2SLS estimation is based a moment which does not exist in finite sample as the coefficient when identified does not have finite variance.

In conclusion, bootstrapping method provides solution to this problem.